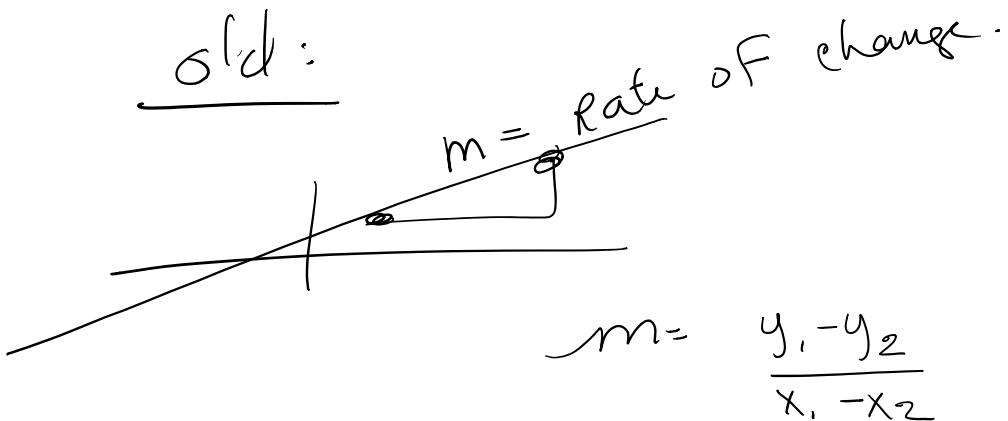


Rate of Change

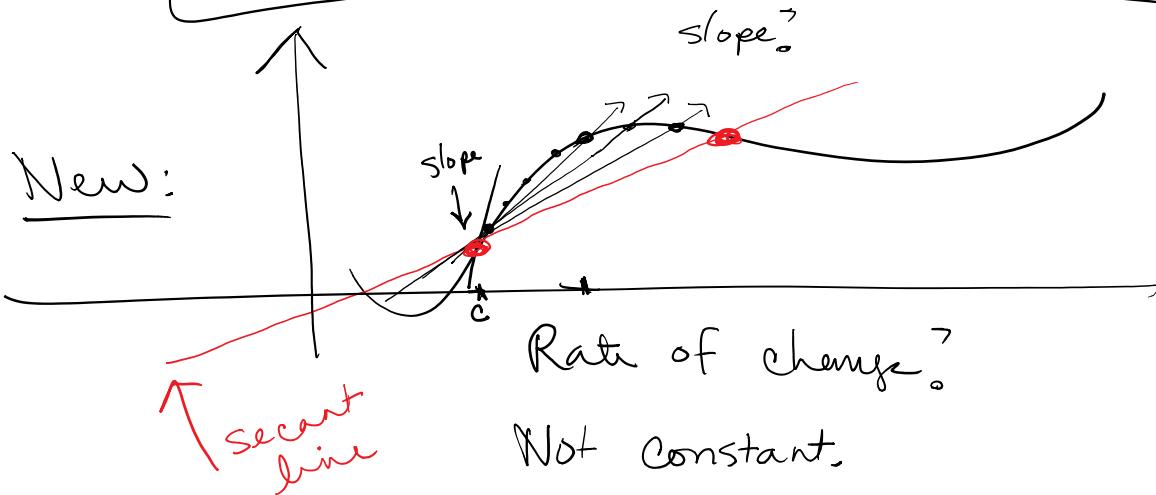
Thursday, September 14, 2017 8:50 AM

Old:



To

$$y - y_1 = m(x - x_1) \quad \text{pt. slope formula.}$$



We will move the right point closer & closer to the point of interest.

* We will squeeze the x values close together.

- (x_2, y_2)

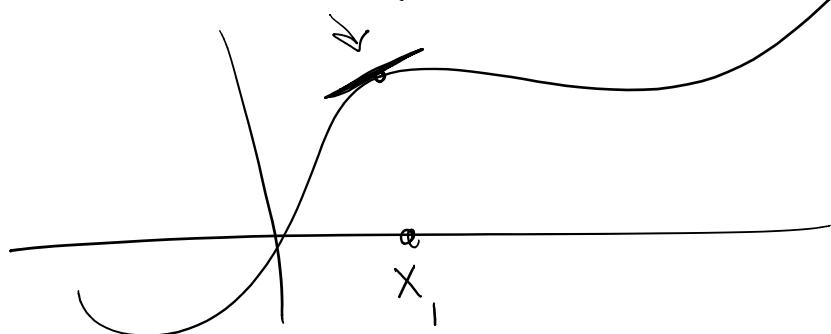
- (x_1, y_1)

$$\lim_{x_2 \rightarrow x_1}$$

$$\frac{y_2 - y_1}{x_2 - x_1}$$

Instantaneous
= Rate
of
Change
at x_1

Tangent line



- The instantaneous rate of change
- The slope of tangent line
- The Derivative

- $\lim_{x \rightarrow c} \frac{f(x) - f(c)}{x - c}$

- $\lim_{\Delta x \rightarrow 0} \frac{f(x + \Delta x) - f(x)}{\Delta x}$

- $\lim_{h \rightarrow 0} \frac{f(x + h) - f(x)}{h}$

old: $(a+b)^3 =$ Binomial Expansion.

$$\begin{array}{cccc} & & 1 & \\ & & | & | \\ 1 & 2 & 1 & \\ & 1 & 3 & 3 & 1 \end{array}$$

$$| a^3 + 3a^2b + 3ab^2 + b^3$$

$$(2x+1)^3$$

$$\begin{array}{cccc} & 1 & 3 & 3 & 1 \\ (2x)^3 1^0 & (2x)^2 1^1 & (2x)^1 1^2 & 1 \cdot 1^3 \end{array}$$

$$8x^3 + 12x^2 + 6x + 1$$

$$f(x) = 3x - 7$$

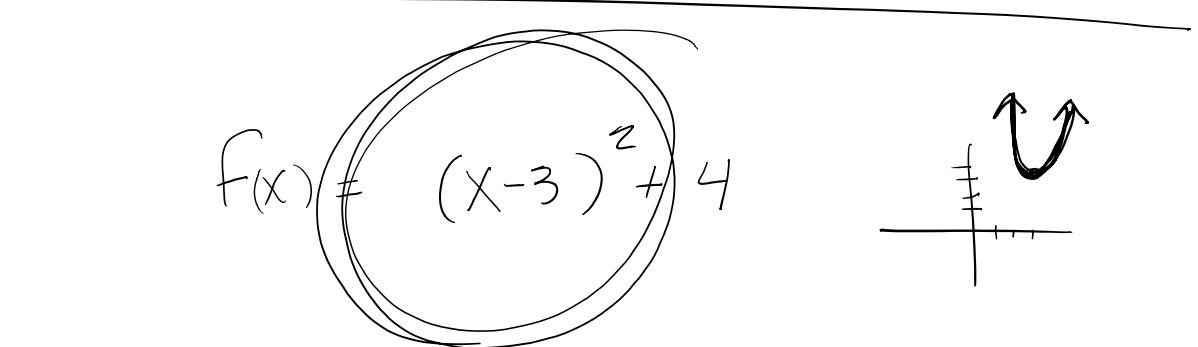
Derivative
 $f'(x) = 3$

$$\therefore f(x+\Delta x) - f(x)$$

$$\lim_{\Delta x \rightarrow 0} \frac{[3(x+\Delta x) - 7] - [3x - 7]}{\Delta x}$$

$$\lim_{\Delta x \rightarrow 0} \frac{3x + 3\Delta x - 7 - 3x + 7}{\Delta x}$$

$$\lim_{\Delta x \rightarrow 0} \frac{3\cancel{\Delta x}}{\cancel{\Delta x}} = 3$$



$$f'(x) = \lim_{\Delta x \rightarrow 0} \frac{f(x+\Delta x) - f(x)}{\Delta x}$$

$$= \lim_{\Delta x \rightarrow 0} \frac{[(x+\Delta x-3)^2 + 4] - [(x-3)^2 + 4]}{\Delta x}$$

$$= \lim_{\Delta x \rightarrow 0} \frac{x^2 + 2x\Delta x - 6x + 4 + (\Delta x)^2 - 3\Delta x}{\Delta x}$$

Algebra

$$= \lim_{\Delta x \rightarrow 0} \frac{x^2 + 2x\cancel{\Delta x} - 6x + (\Delta x)^2 - 3\Delta x + 9}{\Delta x} + 4 - [(x^2 - 6x + 9) + 4]$$

cancel

Algebra

$$\lim_{\Delta x \rightarrow 0} \frac{x^2 + 2x\Delta x - 6x + (\Delta x)^2 - 6\Delta x + 9 + 4 - (x^2 - 6x + 9) - 4}{\Delta x}$$

$$\lim_{\Delta x \rightarrow 0} \frac{\cancel{x^2} + \cancel{2x\Delta x} - \cancel{6x} + \cancel{(\Delta x)^2} - \cancel{6\Delta x} + \cancel{9+4} - \cancel{x^2} + \cancel{6x} - \cancel{9} - \cancel{4}}{\cancel{\Delta x}}$$

$$\lim_{\Delta x \rightarrow 0} \frac{\cancel{x^2} (2x + \cancel{\Delta x} - 6)}{\cancel{\Delta x}} = 0$$

$$f'(x) = 2x - 6$$

a new function.

$$f(x) = (x-3)^2 + 4$$

- $f'(x) = 2x - 6$
- $f'(7) = 8$

- What is equation of tangent line to $(x-3)^2 + 4$ when $x = 7$.

$$m = 8 \\ (7, 20)$$

$$y - 20 = 8(x - 7)$$

$$2, 1, 5, 4, 7, 19, 21, 23,$$

$$25, 26, 81-86$$